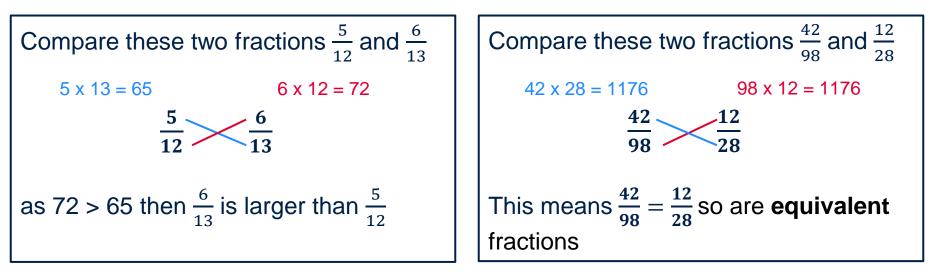


Advanced Mathematics Support Programme®



To order fractions you can use the product of their diagonals



If fractions are equivalent then the product of their diagonals will always be equal!

How could you use this to help you when rearranging expressions or equations with fractions ?



- 1. Rewrite the formula below to make time the subject. Speed = $\frac{\text{Distance}}{1}$
- 2. Rearrange to make *a* the subject of $\frac{x}{y} = \frac{a}{b}$

5. Make *a* the subject of $x = \frac{h+k}{a}$

6. Make *x* the subject of
$$x + a = \frac{x+b}{c}$$

3. Make *x* the subject of $tan\theta = \frac{y}{x}$

7. Make *a* the subject of $\frac{1-a}{1+a} = \frac{x}{y}$

4. These triangles are similar. Show that $x = \frac{cb}{a}$ 8. Make *y* the subject of $y(\sqrt{3} + \sqrt{2}) = x$ and write it in the form $y = x(\sqrt{a} + \sqrt{b})$





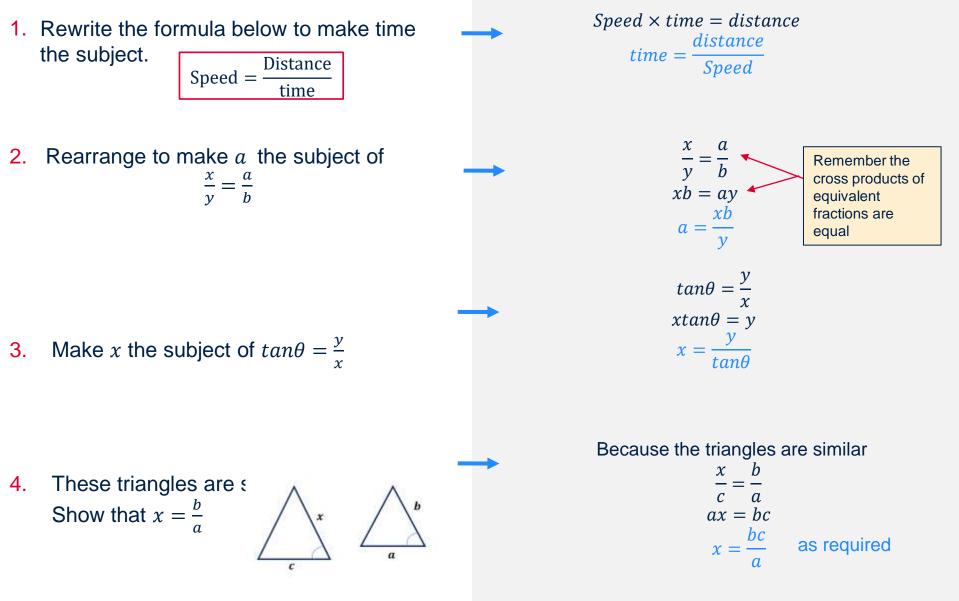
Rearranging Fractions



Solutions on the next slide....

Camsp Rearranging Fractions Solutions





Oamsp Rearranging Fractions Solutions



5.	Make <i>a</i> the subject of $x = \frac{h+k}{a}$		$x = \frac{h+k}{a}$ $xa = h+k$ $a = \frac{h+k}{x}$
6.	Make <i>x</i> the subject of $x + a = \frac{x+b}{c}$		$c(x + a) = x + b$ $cx + ca - x = b$ $cx - x = b - ca$ $x(c - 1) = b - ca$ $x = \frac{b - ca}{c - 1}$
7.	Make <i>a</i> the subject of $\frac{1-a}{1+a} = \frac{x}{y}$	→	y(1-a) = x(1+a) y - ay = x + xa y - x = xa + ay a(x + y) = y - x $a = \frac{y - x}{x + y}$
8.	Make <i>y</i> the subject of $y(\sqrt{3} + \sqrt{2}) = x$ and write it in the form $y = x(\sqrt{a} + \sqrt{b})$		$y = \frac{x}{\sqrt{3} + \sqrt{2}}$ $y = \frac{x}{\sqrt{3} + \sqrt{2}} \times \frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} - \sqrt{2}}$ $y = \frac{x\sqrt{3} - x\sqrt{2}}{3 - 2}$ $y = x(\sqrt{3} - \sqrt{2})$





1. Make *x* the subject of

$$bc = \frac{x}{a}$$

2. Make *e* the subject of

$$x = \frac{y}{e^2}$$

v

3. Write a in terms of x, y, z and b

$$\frac{b-xa}{z} = y$$

4. Make *v* the subject of

$$C = \frac{v^2 - ta}{x}$$

5. Rearrange to make x the subject of $\frac{2}{x} + 5 = 6y$

6. Make *x* the subject of

$$4F = F + \frac{a}{y+x}$$

7. Make *y* the subject of

$$\sqrt{\frac{m(y+a)}{y}} = g$$

8. A cylinder has a radius of 3cm and height, h. The total surface area = $30x \ cm^2$.

Find an expression for the surface area and write *h* in terms of *x* and π





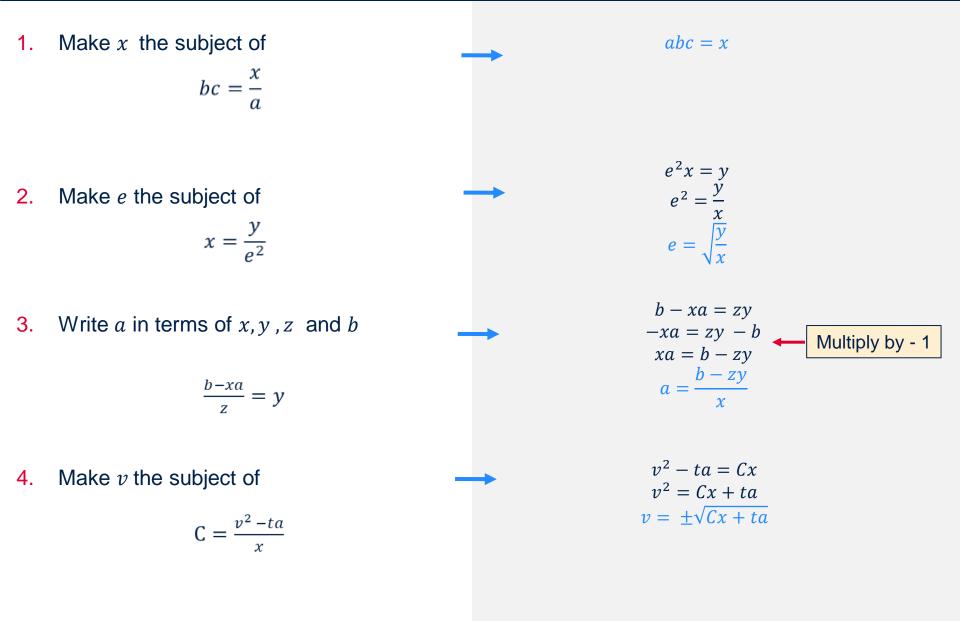
Rearranging Fractions 2



Solutions on the next slide....

Camsp Rearranging Fractions 2 Solutions





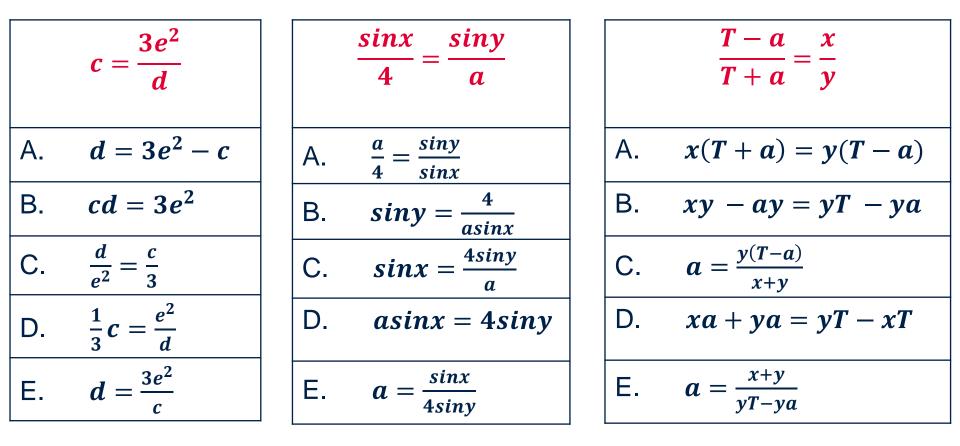
actions 2 Solutions
$\frac{2}{x} = 6y - 5$ $x(6y - 5) = 2$ $x = \frac{2}{6y - 5}$
$3F = \frac{a}{y+x}$ $3Fy + 3Fx = a$ $3Fx = a - 3Fy$ $x = \frac{a - 3FY}{3F}$ $g^{2} = \frac{my + ma}{y}$
$g' = \frac{y}{y}$ $g^{2}y = my + ma$ $g^{2}y - my = ma$ $y(g^{2} - m) = ma$ $y = \frac{ma}{g^{2} - m}$
Surface area of cylinder = $2\pi r^2 + 2\pi rh$ $30x = (2\pi \times 3^2) + (2 \times 3 \times \pi \times h)$ $30x = 18\pi + 6\pi h$ $6\pi h = 30x - 18\pi$ $h = \frac{30x - 18\pi}{6\pi}$ $h = \frac{5x - 3\pi}{\pi}$





Each expression has been rewritten in different ways.

- Which are not correct rearrangements?
- Can you explain what's gone wrong?







Each expression has been rewritten in different ways.

- Which are not correct rearrangements?
- Can you explain what's gone wrong?

$$a - \frac{b^2}{d} = ce$$
A. $b^2 = d(a + ce)$
B. $a = ce + \frac{b^2}{d}$
C. $\frac{b^2}{d} = a - ce$
D. $\frac{b}{\sqrt{d}} = \sqrt{a} - \sqrt{ce}$
E. $b = \pm \sqrt{d(a - ce)}$

$$y + b = \frac{ay + e}{b}$$
A. $by + b^2 = ay + e$
B. $by - ay = e + b^2$
C. $y = \frac{e - b^2}{b - a}$
D. $e = b(y + b) - ay$
E. $y(b - a) = \frac{e - b^2}{y}$





Wrong Steps



Solutions on the next slide....

Each expression has been rewritten in different ways.

- Which are not correct rearrangements?
- Can you explain what's gone wrong?

amsp[®] Wrong Steps Solutions

$$c = \frac{3e^2}{d}$$
A. $d = 3e^2 - c$
B. $cd = 3e^2$
C. $\frac{d}{e^2} = \frac{c}{3}$
D. $\frac{1}{3}c = \frac{e^2}{c}$
E. $d = \frac{3e^2}{c}$

$$\frac{sinx}{4} = \frac{siny}{a}$$
A. $\frac{sinx}{4} = \frac{siny}{sinx}$
A. $\frac{a}{4} = \frac{siny}{sinx}$
B. $siny = \frac{4}{asinx}$
C. $sinx = \frac{4siny}{a}$
D. $\frac{1}{3}c = \frac{e^2}{d}$
E. $a = \frac{sinx}{4siny}$
E. $a = \frac{x+y}{yT-ya}$

Each expression has been rewritten in different ways.

- Which are not correct rearrangements?
- Can you explain what's gone wrong?

amsp[•] Wrong Steps Solutions

$$a - \frac{b^2}{d} = ce$$
A. $b^2 = d(a + ce)$
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D. $\frac{b}{\sqrt{d}} = \sqrt{a} - \sqrt{ce}$
E. $b = \pm \sqrt{d(a - ce)}$

$$y + b = \frac{ay + e}{b}$$
A. $by + b^2 = ay + e$
B. $by - ay = e + b^2$
C. $y = \frac{e - b^2}{b - a}$
D. $e = b(y + b) - ay$
E. $y(b - a) = \frac{e - b^2}{y}$



Prove It!



Using your rearranging skills can you prove each of the following

If
$$a = \frac{b}{b+c}$$

Show that $\frac{a}{1-a} = \frac{b}{c}$

$$\frac{n(n-1)}{2} + \frac{n(n+1)}{2}$$
 is a square number

$$\frac{2x+3}{4} - \frac{3x-2}{3} + \frac{1}{6} = \frac{19-6x}{12}$$





Prove It!



Solutions on the next slide....



Prove It Solutions



	lf	$a = \frac{b}{b+c}$		
	Show that $\frac{a}{a-1} = \frac{b}{c}$			
$\frac{a}{1} = \frac{b}{b+c}$ Make <i>a</i> into a fraction		Make <i>a</i> into a fraction		
a(b+c)=b		Using what we know about the product of the diagonals of equivalent fractions		
ab + ac = b		Expand brackets		
ac = b - ab		Make <i>ac</i> the subject		
$ac = b(1 - a)$ $b = \frac{ac}{1 - a}$		Factorise the right hand side		
		Make <i>b</i> the subject		
$\frac{b}{c} = \frac{c}{1 - c}$	$\frac{b}{c} = \frac{a}{1-a}$ Divide both sides by <i>c</i> , expression as required			



amsp[®] Prove It Solutions



$$\frac{n(n-1)}{2} + \frac{n(n+1)}{2}$$
 is a square number

$\frac{n^2-n}{2} + \frac{n^2+n}{2}$	Expand brackets
$\frac{n^2 - n + n^2 + n}{2}$	Write as one fraction
$\frac{2n^2}{2}$	Simplify numerator
2	
n^2	Cancel out factor of 2 so left with n^2 which is a square number as required



Prove It Solutions



$$\frac{2x+3}{4} - \frac{3x-2}{3} + \frac{1}{6} = \frac{19-6x}{12}$$

Concentrate on Left hand side

Make a common denominator

$$\frac{6x+9}{12} - \frac{12x-8}{12} + \frac{2}{12}$$

Expand brackets

$$\frac{6x+9 - (12x-8) + 2}{12}$$

Collect terms over single denominator

$$\frac{6x + 9 - 12x + 8 + 2}{12}$$

$$\frac{19 - 6x}{12}$$

Simplify

Left hand side is = to right hand side as required





Complete the steps and fill in the blanks to find an expression for the area of triangle ABC

- 1. On the diagram draw a perpendicular line from A to BC
- 2. Label the perpendicular line *h*
- 3. Find an expression for the perpendicular height, h

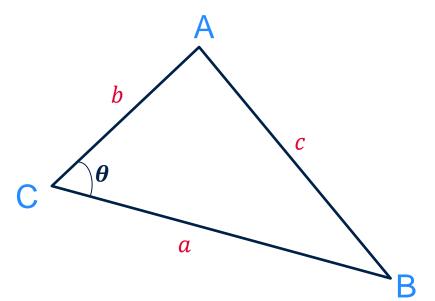
h =

4. Write down the expression for the base of the triangle

base =

5. Write down an expression to find the area of this triangle using your expressions for *base* and *perpendicular height*





Hint: You might want to introduce some trigonometry at step 3.





Missing Steps



Solutions on the next slide....

Oamsp[®] Missing Steps Solutions



Complete the steps and fill in the blanks to find an expression for the area of triangle ABC

- 1. On the diagram draw a perpendicular line from A to BC
- 2. Label the perpendicular line *h*
- 3. Find an expression for the perpendicular height, h

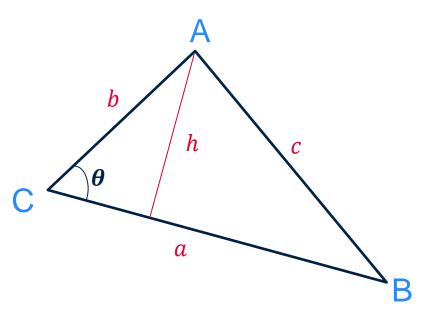
 $Sin\theta = \frac{h}{b}$ so $h = b sin\theta$

4. Write down the expression for the base of the triangle

base = a

5. Write down an expression to find the area of this triangle using your expressions for *base* and *perpendicular height*

Area =
$$\frac{1}{2}$$
 base x perpendicular height
 $A = \frac{1}{2}a \times bsin\theta$ or $A = \frac{1}{2}ab sin\theta$



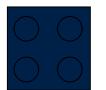




<u>Read</u> about how the rearrangement of algebraic expressions can be used in many real life contexts including proving the quadratic formulae!



Discover how trigonometry was developed to become the study of algebraic ratios from numeric beginnings by comparing the merkhet (not comparing the meerkat!)



<u>Play</u> with Lego, visit Paris and do maths all at the same time? It is possible through Helices!





Contact the AMSP



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