

### Advanced Mathematics Support Programme®



# Trigonometric functions can be used to model many things that repeat over a time period, for example



Tides



**Springs** 



**Harmonic Strings** 



Daylight

### Jamsp Sketching Other Graphs 1

1. What is the mathematical name for the graph of  $y = \frac{1}{x}$ ?

2. What are the maximum and minimum values for the graph  $y = cos\theta$  ?

3. Sketch the graph of  $y = 2^x$ . Label the *y* and *x* intercepts

4. Using a sketch of the graphs  $y = \frac{1}{x}$  and y = xshow how many solutions there will be to the equation  $\frac{1}{x} = x$ 



6. What is the *y* intercept of the graph y = (x + 2)(x - 3)(x + 5)?

7. What are the *x* intercepts of the graph y = (x + 2)(x - 3)(x + 5)?

8. Sketch the graph of y = (x - 3)(x + 2)(x + 5)





#### **Sketching Other Graphs 1**



Solutions on the next slide....

## **Oamsp** Sketching Graphs 1 Solutions





## **Camsp** Sketching Graphs 1 Solutions



- 5. What is the name for this type of graph? A cubic
  - \_\_\_\_\_
- 6. What is the *y* intercept of the graph y = (x + 2)(x 3)(x + 5)?

7. What are the *x* intercepts of the graph y = (x + 2)(x - 3)(x + 5)?

8. Sketch the graph of y = (x - 3)(x + 2)(x + 5) y intercept when x = 0 y = (0+2)(0-3)(0+5)  $y = 2 \times (-3) \times 5$  y = -30y intercept at (0, -30)

x intercepts when y = 0 0 = (x + 2)(x - 3)(x + 5) x = -2 and x = 3 and x = -5x intercepts at (-2,0) (3,0) (-5,0)



Unsure about any of these? Search - Identifying Graphs. Next try Sketching graphs 2....





1. What is the mathematical name for graphs of the form of  $x^2 + y^2 = 9$ ?

2. Sketch the graph of  $y = sin\theta$  between 0° and 360°, labelling x and y intercepts

- 3. On your sketch for Q2 draw in the line y = 0.5How many solutions are there to  $sin\theta = 0.5$ ? Can you say what they are?
- 4. Sketch the graph  $y = x^3$ , labelling any intersections

- Sketch the graph of the equation in Q1, label any intersections with the *x* and *y* axis
- 6. What is the *y* intercept of the graph y = (x + 1)(x + 1)(x 1)?

7. What are the *x* intercepts of the graph y = (x + 1)(x + 1)(x - 1)?

8. Sketch the graphs of  $x^2 + y^2 = 4$  y = x + 1Use the sketch to determine how many solutions there are when those

equations are solved simultaneously





#### **Sketching Graphs 2**



Solutions on the next slide....

#### Sketching Graphs 2 Solutions



1. What is the mathematical name for graphs of the form of  $x^2 + y^2 = 9$ ?

Circles are of the form  $x^2 + y^2 = r^2$ 





3. On your sketch for Q2 draw in the line y = 0.5How many solutions are there to  $sin\theta = 0.5$ ? Can you say what they are?



Two solutions 30° and 150° The points of intersection

4. Sketch the graph  $y = x^3$ , labelling any intersections



## **Oamsp** Sketching Graphs 2 Solutions



- 5. Sketch the graph of the equation in Q1. Label any intersections with the *x* and *y* axis
- 6. What is the *y*-intercept of the graph y = (x + 1)(x + 1)(x 1)?

- 7. What are the *x* intercepts of the graph y = (x + 1)(x + 1)(x 1)?
- Raduo = 3 y intercept when x = 0y = (0+1)(0+1)(0-1) $y = 1 \times 1 \times -1$ v = -1y intercept is (0, -1)x intercept when y = 00 = (x + 1)(x + 1)(x - 1)x = -1 x = 1x intercept is (-1,0) repeated and (1,0)in de contre 100 radius 2

8. Sketch the graphs of

 $x^{2} + y^{2} = 4$ y = x + 1

Use the sketch to determine how many solutions there are when those equations are solved simultaneously



#### Two solutions



#### Which is which?



Match the graphs to the equations There are more equations than you need!







#### Which is which?



Solutions on the next slide....



Which is which?



#### Match the graphs to the equations



## **Oamsp** Sketching more than graphs



Find the shortest distance between the following curves:  $x^2 + y^2 = 9$  $y = x^2 + 7$ 

A car is initially travelling at 300m/min, it speeds up over a 20 second interval with a constant acceleration to achieve a speed of 400m/min. It travels at this speed for 3 minutes before slowing to a stop via constant de-acceleration over a period of 30 seconds.

a) What is the car's average speed for the first 20 seconds of travel?b) What is the car's deceleration?

A square is placed inside a circle  $(C_1)$  so that the corners perfectly touch the circle's circumference.

Another circle  $(C_2)$  is now placed inside this square so that its circumference perfectly touches the square's sides.

What is the ratio of the lengths of the radius of  $C_1$  and the radius of  $C_2$ ?

Hint: Assume C<sub>2</sub> has a radius of 1 unit





#### Sketching more than graphs



Solutions on the next slides....

### **Oamsp**<sup>®</sup> Sketching more than graphs Solution



#### **Oamsp**<sup>®</sup> Sketching more than graphs Solution



A car is initially travelling at 300m/min, it speeds up over a 20 second interval with a constant acceleration to achieve a speed of 400 m/min.

It travels at this speed for 3 minutes before slowing to a stop via constant de-acceleration over a period of 30 seconds.

Diagram not to scale





# **Oamsp**<sup>\*</sup> Sketching more than graphs Solution



#### a) What is the cars' average speed for the first 20 seconds of travel?

Drawing the blue horizontal line on the graph is a visual way to show that the average speed is half way between 300m/min and 400m/min which is 350m/min

#### b) What is the cars' deceleration?

By drawing in the red lines we can see that it takes 30 secs for the car to stop - after travelling at 400m/min. (30 seconds = 0.5 minutes), so ... Deceleration =  $400 \div 0.5 = 800$ m/min<sup>2</sup>

#### **Oamsp**<sup>\*</sup> Sketching more than graphs Solution



A square is placed inside a circle  $(C_1)$  so that the corners perfectly touch the circle's circumference.

Another circle  $(C_2)$  is now placed inside this square so that its circumference perfectly touches the square's sides.

What is the ratio of the lengths of the radius of  $C_1$  and the radius of  $C_2$ ?





#### Challenge ahead!





The activities on the next few slides may contain some content from A level maths; for that reason they are optional, but still fun and worth trying!





Solve (sin x + 1)(2cos x - 1) = 0 for  $0 < x < 360^{\circ}$ 





### A Triggy Problem



Solutions on the next slide....

amsp<sup>®</sup> Triggy Problems Solutions



Solve  $(\sin x + 1)(2\cos x - 1) = 0$  for  $0 < x < 360^{\circ}$ 

Fortunately, this is an already factorised quadratic. So.....







Which one of the equations below describes the graph?

- y = (x+1)(x-1)(x-2)
- y = -x(x-1)(x+1)
- y = x(x-1)(x+1)







#### A cubic match up



Solutions on the next slides....

## Camsp A cubic match up Solution

#### Which one of the equations below describes the graph?



The correct equation is y = x(x - 1)(x + 1)



Extend what you have learnt about quadratics to help you match up the cubic graphs in this Desmos activity

Learn more about factorising cubics in this activity – with solutions





#### Click here to try our Exponential Marbleslides Challenge

#### You will be investigating the features of exponential graphs whilst trying to catch as many stars as possible



You can join the activity without signing in or entering your real name.





Read about Euclid's Axioms and discover how they might be used in this interactivity. Sketches and diagrams help with more than just questions about graphs!



Play 'Euclidea' to explore more about Euclidean Geometry and constructions.



Watch this video to see how you can 'graph' art! To see all the finalists in the Desmos Art competition (and get inspiration to enter it yourself in the future) click <u>here</u>.





# Contact the AMSP



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