

## Advanced Mathematics Support Programme®



#### Quadratic curves are also known as parabolas. Parabolas are used in many examples of architecture.







- Do you recognise these landmarks?
- Do you think they are parabolas?





Quadratic Graphs 1



Find the coordinates of A, B and C etc.. on each graph











 $y = (x - 1)^2 + 4$ 

AE Version 2.0 11/09/18.

 $y = (x + 3)^2 + 7$   $y = x^2 + 3x - 4$   $y = 2x^2 + 4x - 6$ 





## **Quadratic Graphs 1**



Solutions on the next slide....





$$B(-3,0)$$
 $B(-2,0)$  $B(-1,0)$  $C(0,-6)$  $C(0,-6)$  $C(0,-5)$ 

Unsure about any of these? Search Sketching Quadratic Graphs. Next try Quadratics Graphs 2....

B(-5,0)

C(0, -20)

## **Oamsp** Quadratic Graphs 1 Solutions





For this equation you need to complete the square to find the minimum point D

Unsure about any of these? Search Sketching Quadratic Graphs. Next try Quadratic Graphs 2....





In mathematics a sketch does not need to be a completely accurate drawing, but it should "illustrate all the significant features of the graph/shape"

0

What do you think the significant or key features of a quadratic graph are?

What techniques have you used so far that can help you find those key features?



#### Label it!



These diagrams show the key features of a quadratic graph



Put the words below into the boxes above so that the quadratic graphs are labelled correctly. Some words may be used more than once.







### Label it!



Solutions on the next slide....





#### These diagrams show the key features of a quadratic graph



N.B. In mathematics a sketch does not need to be a completely accurate drawing, but it must illustrate all the significant features of the graph/shape.



**Identification Parade** 



• Which of the following graphs is  $y = x^2 - 5x + 4$ 











### **Identification Parade**



Solutions on the next slide....

## **Camsp**<sup>®</sup> Identification Parade Solution



So the correct graph has x intercepts (1,0) and (4,0) and y intercept (0,4)



The red graph has the correct x intercepts but it has a y intercept at (0,8)





The blue graph has the correct y intercept only

The graph above is  $y = x^2 - 5x + 4$ 





Look at the two graphs below.

• Can you describe how to move Graph A onto Graph B?

GRAPH A





Can you see how that links to the equation of the graph?





• Can you describe how to move Graph A onto Graph B?



Which transformations would take GRAPH A onto each of the graphs below?











### Move it!



Solutions on the next slide....



### Move it! Solutions









Look at the new graphs below.

• Can you describe how to move Graph A onto Graph B?



**GRAPH B** 



Can you see how that links to the equation of the graph?





Can you describe how to move Graph A onto Graph B?



Minimum coordinate at (4,3)

Completing the square gives us the coordinate of the minimum point of the graph and it also gives us the translation from  $y = x^2$  to another quadratic graph

Completing the square form is very useful for all types of questions involving quadratics and circles at A level

## **Oamsp** Complete the square to get sorted!



Draw out a 3 by 3 grid like this one that's large enough to write the equations in	You have been given 10 equations. Your task is to place 9 of them onto the grid according to these rules on the cards	The turning point of the equation $y = (x + a)^2 + b$ is at $(-a, b)$	All of the coordinates of the turning points are at integer values of <i>x</i> and <i>y</i> . None of the turning points are on either axis.
All of the equations in the top row have a turning point on the line $y = 4$	One of the equations in the left hand column has its turning point at (-4, 4)	The equation with a turning point at (-1, 4) is not on the top row	The equations in the top left and centre right square both have the same y coordinate for their turning point
All three of the equations with a turning point on the line $x = 3$ are on the bottom row	All of the equations in the centre column have turning points on the line $y = 5 - x$	All of the turning points for the equations in the centre column are in the first quadrant	$y = x^{2} + 6x + 10$ is in the square in the left hand column directly above $y = x^{2} - 6x + 16$
The equations to sort are:		$y = x^2 - 4x + 7$	$y = x^2 + 2x + 5$
$y = x^2 - 6x + 16$	$y = x^2 - 6x + 25$	$y = x^2 - 2x + 5$	$y = x^2 + 8x + 20$
$y = x^2 - 6x + 11$	$y = x^2 - 8x + 21$	$y = x^2 + 6x + 10$	$y = x^2 - 10x + 29$





#### Complete the square to get sorted!



Solutions on the next slide....









1. What are the *x* intercepts of

y = (2x+3)(x+4)

2. What are the *x* and *y* intercepts of this graph.



3. Write the equation of the graph in the form  $ax^2 + bx + c$ 



4. What are the *x* intercepts of the graph of  $y = 6x^2 + x - 2$ 

- 5. What does the *c* part of the equation in  $y = ax^2 + bx + c$  represent on a graph?
- 6. Sketch the graph of  $y = 3x^2 2x 8$ . Label x and y intercepts

7. What are the co-ordinates of the points marked on the diagram of the equation  $y = x^2 + 6x + 16$ 

8. Which of these statements about the graph  $y = x^2 - 4x + 8$  are true







### **Quadratic Graphs 2**



Solutions on the next slide....

## **Oamsp** Quadratic Graphs 2 Solutions



1. What is the *x* intercept of

y = (2x+3)(x+4)

2. What are the x and y intercepts of this graph.



3. Write the equation of the graph in the form  $ax^2 + bx + c$ 



(2x+3)(x+4) = 0 $x = -\frac{3}{2}$  x = -4x intercepts are  $(-\frac{3}{2}, 0)$  and (-4, 0)

x intercepts are (-3, 0) and (2, 0)

y intercepts is (0, -6)

x intercepts are (-2, 0) and (3, 0)which come from (x + 2)(x - 3) = 0expanding gives  $x^2 - x - 6 = y$ 

 $6x^{2} + x - 2 = 0$ (3x + 2)(2x - 1) = 0 x intercepts are  $\left(-\frac{2}{3}, 0\right)$  and  $\left(\frac{1}{2}, 0\right)$ 

4. What are the *x* intercepts of the graph  $y = 6x^2 + x - 2$ 

## **Oamsp** Quadratic Graphs 2 Solutions









The height of a ball thrown up from the ground into the air at time, *t*, is given by:

 $h = 20t - 10t^2$ 



- Find when the ball hits the ground
- How long is the ball more than 5m above the ground?
- Find the maximum height reached by the ball





## How High?



Solutions on the next slide....

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## How High? Solution







Inequalities reminder





Rearrange into factorised form...

(x-5)(x+1) < 0

...now you can sketch the graph

When x > -1 and x < 5 the curve is below the *x* axis.



This is one region, so can be represented by one inequality -1 < x < 5



Inequalities reminder





Rearrange into factorised form...

When x < -1 and x > 5the curve is above the x axis.



These are two regions, so are represented by two inequalities x < -1 and x > 5





#### Use a sketch to help you solve the following inequalities

1. 
$$(x-2)(x+3) < 0$$

**2.** 
$$(4+x)(2-x) < 0$$

**3.** 
$$x^2 + 7x + 12 \ge 0$$

**4.** 
$$(x+2)^2 \le 36$$





### **Quadratic Inequalities**



Solutions on the next slide....

## **Oamsp** Quadratic Inequalities Solutions







#### Fill the table



Sketch	Equation	x intercept	y intercept	Minimum point
-4 1				
		(5,0) (-2,0)	(0, -10)	
				(-5, 6)
	$y = x^2 + 6x + 8$		(0,8)	





### Fill the table



Solutions on the next slide....



## Fill the table Solutions



Sketch	Equation	x intercept	y intercept	Minimum point
-4 1	y = (x + 4)(x - 1) y = x <sup>2</sup> + 3x - 4	(-4,0)(1,0)	(0, -4)	$\left(x + \frac{3}{2}\right)^2 - \frac{9}{4} - 4$ $\left(x + \frac{3}{2}\right)^2 - \frac{25}{4}$ Min point $\left(-\frac{3}{2}, -\frac{25}{4}\right)$
(-2, 0) $(5, 0)(0, -10)$ $(1, 5, -12, 25)$	y = (x - 5)(x + 2) $y = x^2 - 3x - 10$	(5,0)(-2,0)	(0, -10)	$\left(x - \frac{3}{2}\right)^2 - \frac{9}{4} - 10$ $\left(x - \frac{3}{2}\right)^2 - \frac{49}{4}$ Min point $\left(\frac{3}{2}, -\frac{49}{4}\right)$
(4), 753 3 90 60 60 60 60	$y = (x + 5)^{2} + 6$ $y = x^{2} + 10x + 31$	Sits above x axis so no intercepts	(0,31)	(-5, 6)
(-2,0) (-2,0) (-1,0)	$y = x^2 + 6x + 8$	(-4,0)(-2,0)	(0,8)	$(x+3)^2 - 9 + 8$ $(x+3)^2 - 1$ Min point (-3, -1)





#### Click <u>here</u> to try a Quadratic Marbleslides Challenge

You will be investigating the features of quadratic graphs whilst trying to catch as many stars as possible



You can join the activity without signing in or entering your real name.







<u>Download</u> the app and challenge yourself to find the mystery graphs with this game from MEI. Will you take your time or compete against the clock?



Discover more about parabolas and their use, including their use in mirrors and satellite dishes.



Watch this video and learn how getting your paraboloid wrong can have some very unintended consequences! The video includes a little bit of A Level maths content.





# Contact the AMSP



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